

# Modelling a Network of Decision Makers

Dr Tim Gardener

**Professor Jim Moffat** 

Dr Chris Pernin (RAND)

June 2004

maintaining the data needed, and c including suggestions for reducing	ompleting and reviewing the collect this burden, to Washington Headqu uld be aware that notwithstanding ar	o average 1 hour per response, includion of information. Send comments a arters Services, Directorate for Informy other provision of law, no person a	regarding this burden estimate mation Operations and Reports	or any other aspect of the 1215 Jefferson Davis	is collection of information, Highway, Suite 1204, Arlington	
1. REPORT DATE JUN 2004		2. REPORT TYPE		3. DATES COVERED <b>00-00-2004 to 00-00-2004</b>		
4. TITLE AND SUBTITLE				5a. CONTRACT NUMBER		
Modelling a Netowrk of Decision Makers (Briefing Charts)				5b. GRANT NUMBER		
				5c. PROGRAM ELEMENT NUMBER		
6. AUTHOR(S)				5d. PROJECT NUMBER		
				5e. TASK NUMBER		
				5f. WORK UNIT NUMBER		
7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES)  Defence Science and Technology Laboratory, Dstl Farnborough, Ively Road, Farnborough, Hampshire GU14 0LX United Kingdom,				8. PERFORMING ORGANIZATION REPORT NUMBER		
9. SPONSORING/MONITORING AGENCY NAME(S) AND ADDRESS(ES)				10. SPONSOR/MONITOR'S ACRONYM(S)		
				11. SPONSOR/MONITOR'S REPORT NUMBER(S)		
12. DISTRIBUTION/AVAILABILITY STATEMENT  Approved for public release; distribution unlimited						
13. SUPPLEMENTARY NO <b>The original docum</b>	otes nent contains color i	mages.				
14. ABSTRACT						
15. SUBJECT TERMS						
16. SECURITY CLASSIFIC	17. LIMITATION OF ABSTRACT	18. NUMBER OF PAGES	19a. NAME OF			
a. REPORT unclassified	b. ABSTRACT <b>unclassified</b>	c. THIS PAGE unclassified	ABSTRACT	31	RESPONSIBLE PERSON	

**Report Documentation Page** 

Form Approved OMB No. 0704-0188

#### Acknowledgements

 This work is based on the RAND publication "Information Sharing in Military Headquarters: the Impact on Decision Making" by

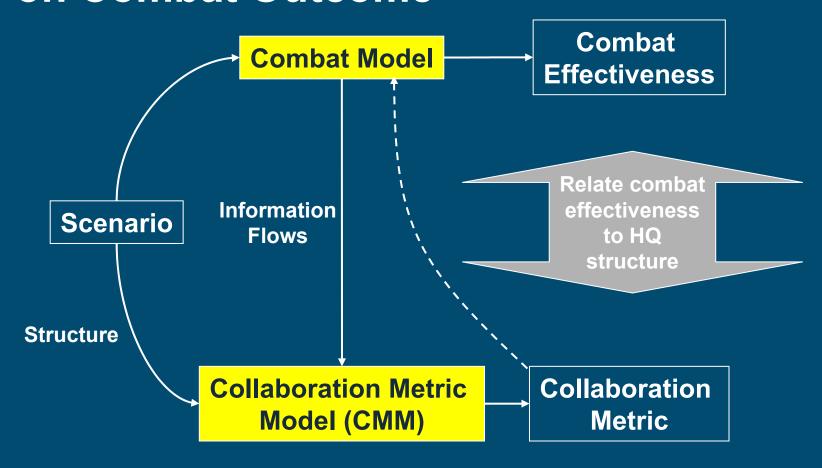
Dr Walt Perry (RAND) and Prof Jim Moffat (Dstl)

Funded by Directorate Equipment Plan, Ministry of Defence, UK





## Testing the impact of shared information on Combat Outcome



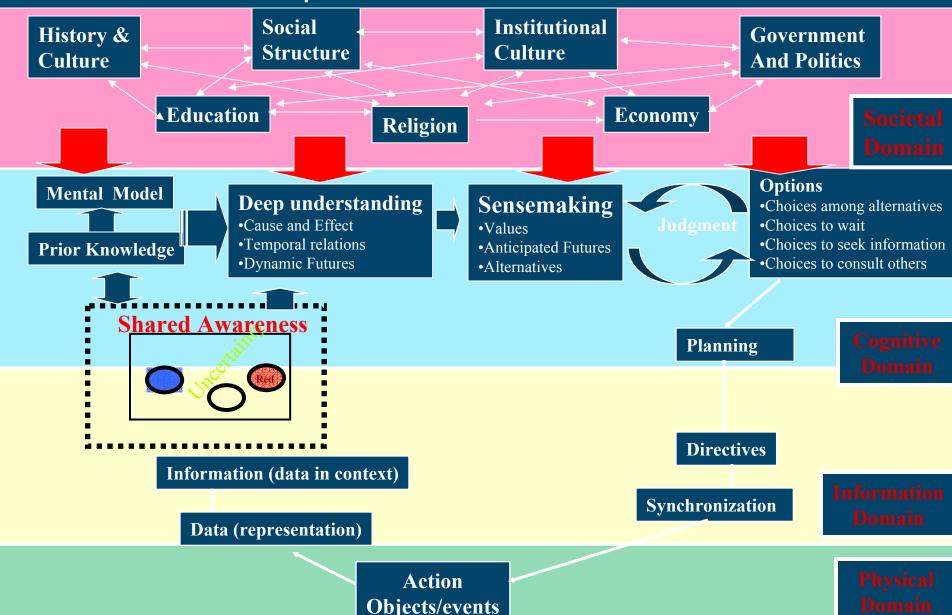






### Physical - Information - Cognitive - Societal

**Ed Smith "Effects Based Operations"** 



#### Some simplifying assumptions

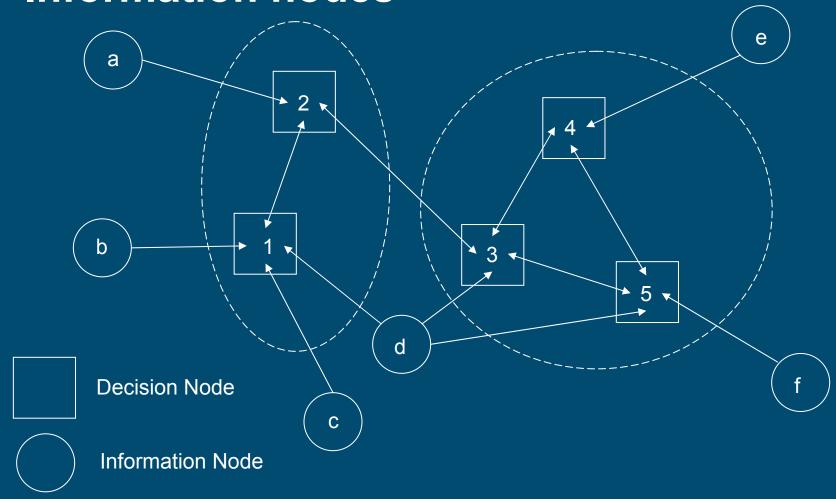
- Focus on the Information Domain and the Cognitive Domain
- Network comprises nodes and edges between nodes together with flows through the graph
- There are two types of node
  - Decision Making node
  - Information node
- There may be several different flows simultaneously







### Network of decision making nodes and Information nodes





Includes Crown Copyright

Materiel

Dstl/CP/11051

30 September

2004

# Cognitive Domain The Recognition Primed Decision Model

A decision is simply the selection of a Course of Action in response to a situation

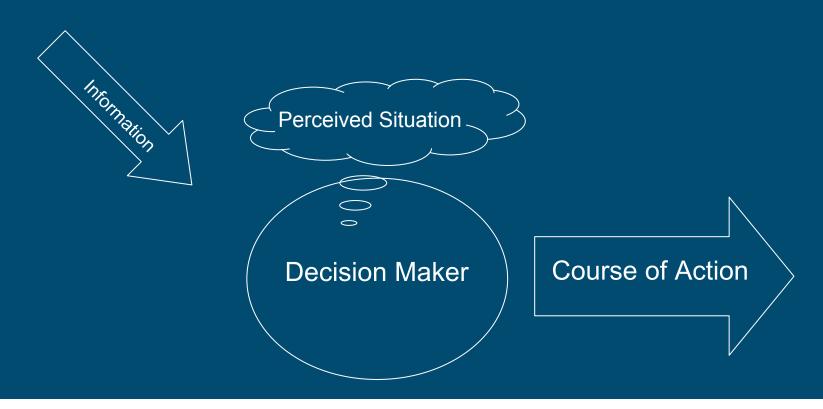








More accurately, the decision maker bases his decision on perception of the situation



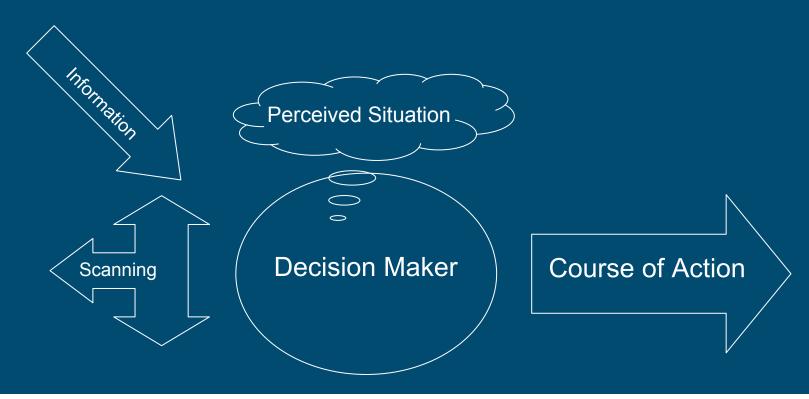






The decision maker scans the environment for clues and cues that might clarify his perception of the given situation

**Key Information Requirements** 

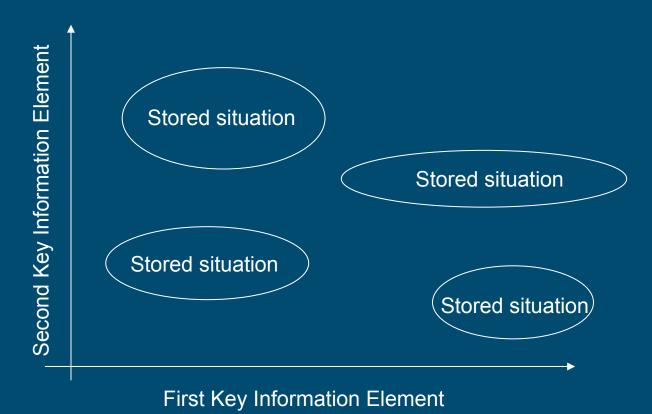








Situations from experience are stored in the decision maker's mind Each experience is labelled by a region in the "Information Element Space" To each stored situation is associated a Course of Action

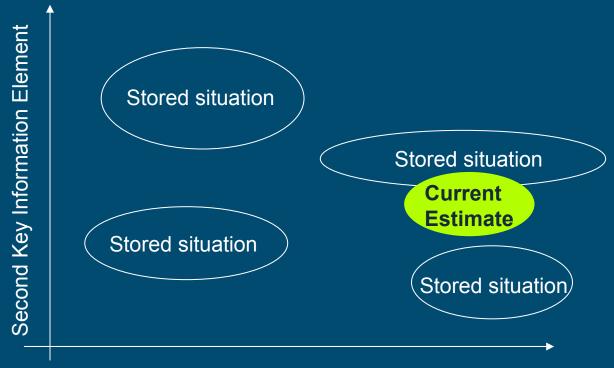








The decision maker's estimate of the current situation is plotted in the Information Element Space - with a volume of uncertainty





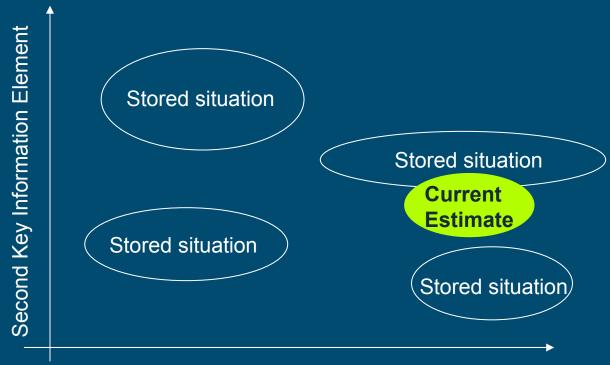






How closely must the perceived situation match a stored situation for the stored Course of Action to be chosen?

Is the decision maker feeling lucky?



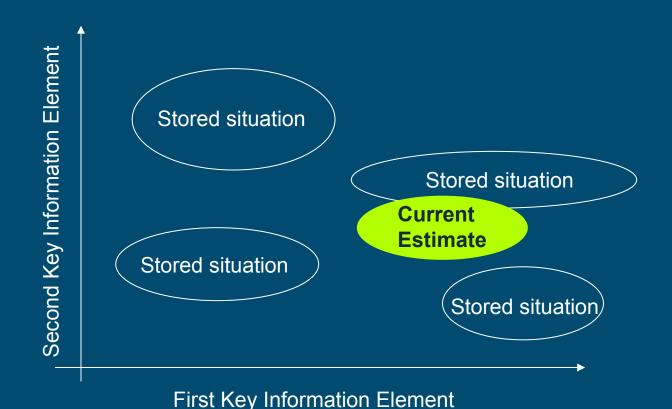
First Key Information Element







As time goes by, the estimate will change and the degree of uncertainty may increase

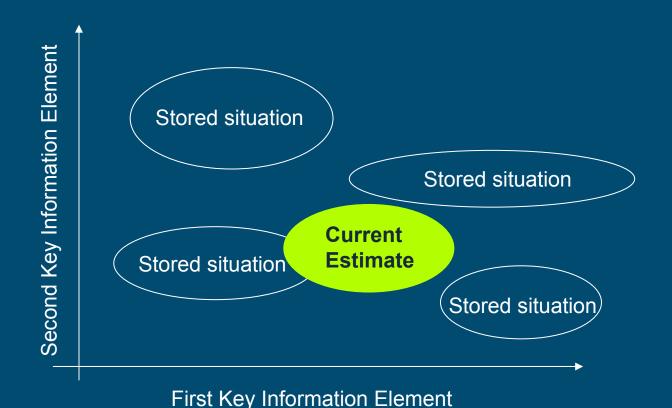








As time goes by, the estimate will change and the degree of uncertainty may increase

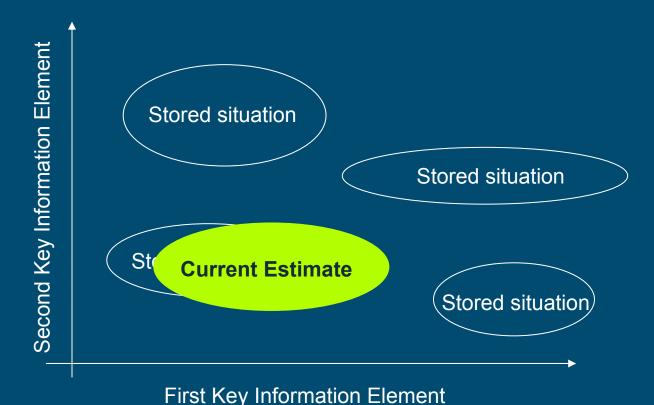








As time goes by, the estimate will change and the degree of uncertainty may increase - until a change in the course of action is desirable or inescapable

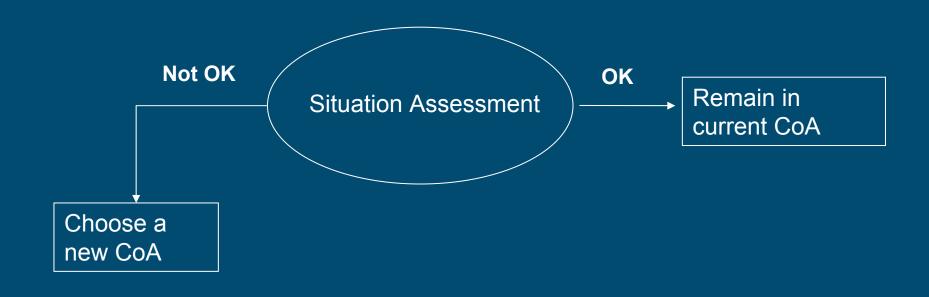








Situation assessment - OK / Not OK









## Information domain - Representing **Uncertainty**

Information Element Space is spanned by a small number of critical information elements  $\mathbf{A} = \{a_1, \dots, a_N\}$ 

**Example:**  $A = \{ \text{location, altitude, speed, direction, missile type} \} = \{ \mathbf{a}_1, a_2, a_3, a_4, a_5 \} \}$ 

Each of these information elements is given by a probability distribution

The mean vector represents current estimate  $\mu = [\mu_1, \mu_2, \Lambda, \mu_N]$ 

$$\mathbf{\mu} = \left[\mu_1, \mu_2, \Lambda_1, \mu_N\right]$$

The covariance matrix of the multivariate distribution represents

uncertainty

$$\boldsymbol{\Sigma} = \begin{bmatrix} \sigma_1^2 & \boldsymbol{\Sigma}_{1,2} & \boldsymbol{\Lambda} & \boldsymbol{\Sigma}_{1,N} \\ \boldsymbol{\Sigma}_{2,1} & \sigma_2^2 & \boldsymbol{\Lambda} & \boldsymbol{\Sigma}_{2,N} \\ \mathbf{M} & \mathbf{M} & \mathbf{O} & \mathbf{M} \\ \boldsymbol{\Sigma}_{N,1} & \boldsymbol{\Sigma}_{N,2} & \boldsymbol{\Lambda} & \sigma_N^2 \end{bmatrix}$$







#### Representing Uncertainty

Decisions depend on the confidence of the decision maker in the accuracy of the estimation

A measure of Uncertainty from Shannon's *Theory of Information* is **Information Entropy** 

The Information Entropy contained in a joint probability density function **f**(**X**) is given by

$$H(\mathbf{X}) = E[-\log f(\mathbf{X})] = -\iint_{x_1, x_2} \Lambda \int_{x_N} f(\mathbf{X}) \log f(\mathbf{X}) dx_N \Lambda dx_2 dx_1$$







#### Representing Uncertainty

Decisions depend on the confidence of the decision maker in the accuracy of the estimation

A measure of Uncertainty from Shannon's *Theory of Information* is **Information Entropy** 

The Information Entropy contained in a multivariate normal distribution was calculated by Shannon in 1948.

$$H(\mathbf{X}) = \frac{1}{2}\log(2\pi)^{N} |\mathbf{\Sigma}| + \frac{N}{2} = \frac{1}{2}\log[(2\pi e)^{N} |\mathbf{\Sigma}|],$$







#### Metrics - How good is my information?

- Precision function of the covariance
- Accuracy function of the mean
- Completeness measure of how critical are the critical information requirements?

These are combined into one single metric - the Collaboration Measure







#### Some Effects of Collaboration

Sharing information reduces uncertainty and leads to greater precision, greater accuracy

Sharing information ———> more complete information





#### Some Effects of Collaboration

Sharing information reduces uncertainty and leads to greater precision, greater accuracy

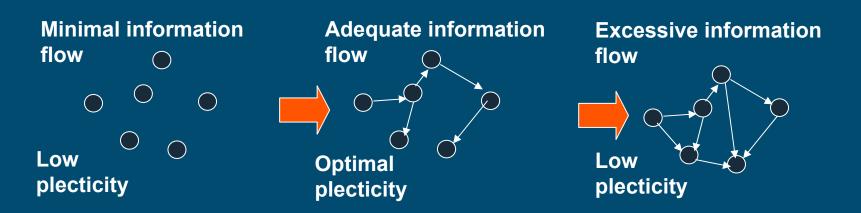
Sharing information cost - time, volume, disconfirming evidence





#### Metrics - How good is my network?

- Network Redundancy measure of the reliability of the network
  - this is simultaneously a cost and a benefit
- Access Cost connectivity score based on the distance piece of information must travel from source to decision maker
- Information Overload Cost measure of the process time required to distinguish between needed and unneeded information









#### **Metrics**

**Information Metrics** 

**Network Metrics** 

Accuracy

Precision

Completeness

Information Accessibily
Network Redundancy
Information Overload

COLLABORATION

**PLECTICITY** 

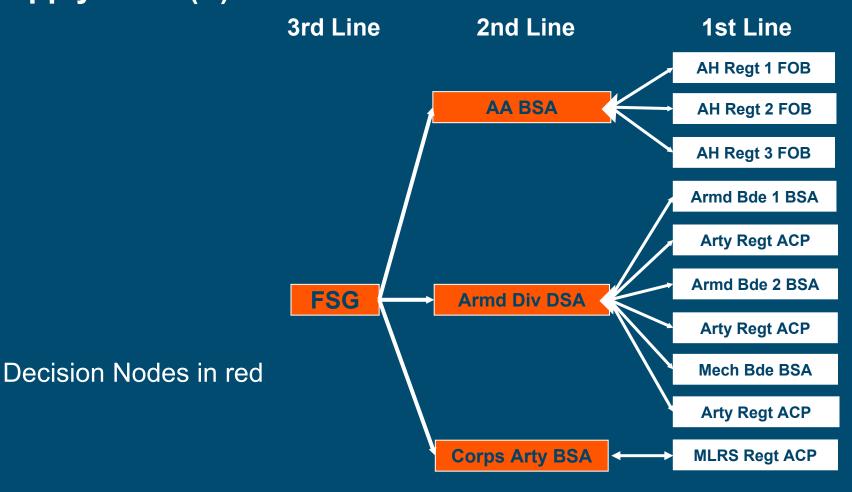
OVERALL NETWORK EFFECTIVENESS







## First Network of Decision Makers Supply Case (S)



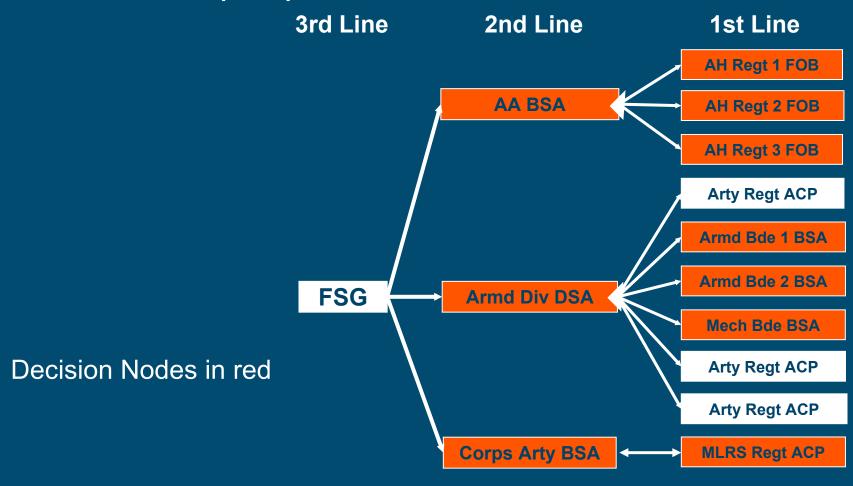






## **Second Network of Decision Makers**

**Demand Case (D10)** 



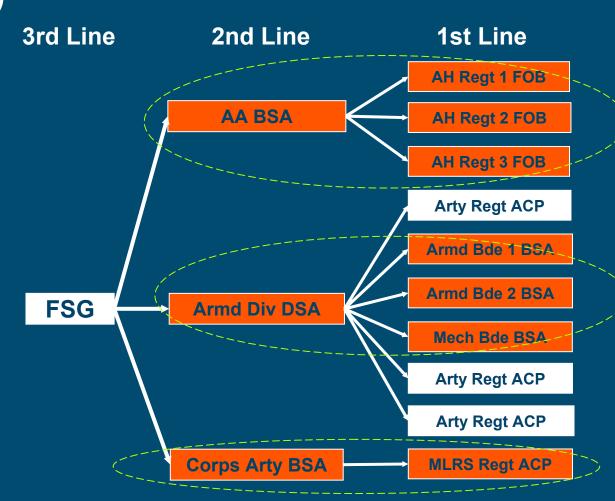






#### **Third Network of Decision Makers**

**Demand Case (D3)** 



Decision Nodes in red Clusters in green







#### Input data from the combat model

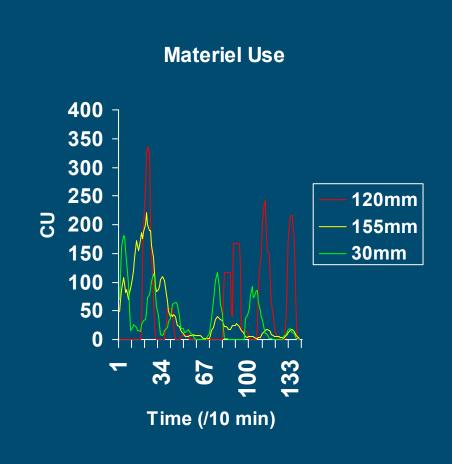
- Actual use and Consumption Unit data for Ammo and Supplies:
  - 120mm, 155mm, 30 mm,81mm
  - MLRS, HellFire
  - Fuel, Oil+Lub, PW, Rations, Bulk Water
- Variety of first, second and third line log units

Includes Crown Copyright

Time steps from 1 minute increment

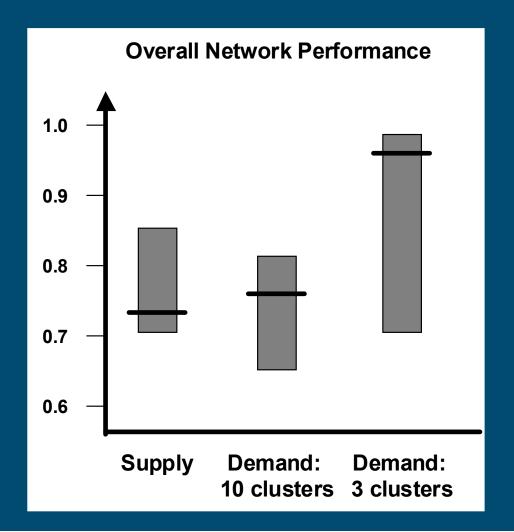
Materiel

Dstl/CP/11051





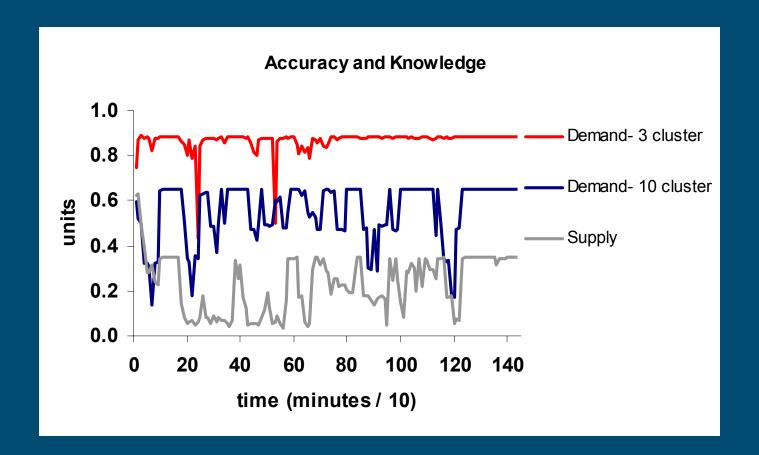










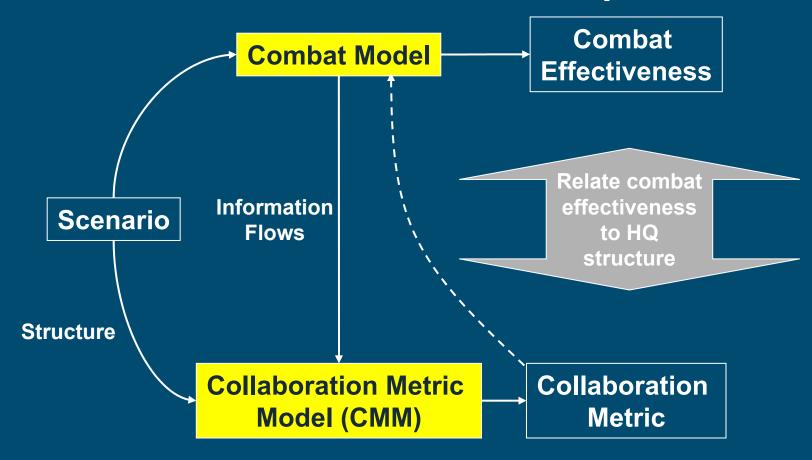








# Study Diagram CMM / Combat Model Relationship





Includes Crown Copyright

Materiel

Dstl/CP/11051



